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1 ### Cloning_randomtimes_constant-pop.py
2
3 import random, math, pylab, heapq
4         # heapq provides the Heap Queue structure which allows to manipulate efficiently
5         # sorted list.
6         # Here we use a list of copies of the system, sorted according to their next time
7         # of evolution.
8 c=.25      # c = creation rate 0->1 ; 1-c = annihilation rate 1->0
9 s=0.30     # s conjugated to the activity K
10 t=0.      # initial and maximal time
11 popsize=400 # population size
12 populat=[]
13         # initial state of the population :
14         # each member of (or "copy" in) the population is described by a 3-uple
15         # (time,dt,state)
16         # time = next time at which it will evolve
17         # dt = time since last evolution
18         # state = 0 or 1 = empty or occupied
19 tmax=2000. # maximal time
20 tmin=tmax/2 # measures start at tmin
21 step=0     # counter for the number of steps in the "mutation/selection" process
22
23 # s-modified escape rate
24 def sescape(n):
25     if n==0:
26         esc=c*math.exp(-s)
27     else:
28         esc=(1-c)*math.exp(-s)
29     return esc
30
31 # s-dependent cloning rate
32 def cloningrate(n): # always positive, as we took s<0
33     if n==0:
34         rate=c*(math.exp(-s)-1.)
35     else:
36         rate=(1.-c)*(math.exp(-s)-1.)
37     return rate
38
39 # procedure to remove a element of index i from a heap, keeping the heap structure intact
40 def heapq_remove(heap, index):
41     # Move slot to be removed to top of heap
42     while index > 0:
43         up = (index + 1) / 2 - 1
44         heap[index] = heap[up]
45         index = up
46     # Remove top of heap and restore heap property
47     heapq.heappop(heap)
48
49 # lists to sample the logarithm of the cloning ratios Y a function of time
50 sampletime,samplesY,samplesYint=[],[],[]
51 Y,Yint=0.,0.
52
53 # initialization of the population
54 populat=[ (0.,0.,random.randint(0,1)) for count in range(popsize)]
55 heapq.heapify(populat) # orders the population into a Heap Queue
56
57 while t<tmax:
58     # we pop the first element of populat, which is always the next to evolve
59     (t,dt,state)=heapq.heappop(populat)
60     # the copy we popped out is to be replaced by p copies ; random.random() is uniform on [0,1[
61     cloningfactor= math.exp(dt*cloningrate(state))
62     p=int( cloningfactor + random.random() )
63
64     if p==0: # one copy chosen at random replaces the current copy
65         toclone=random.choice(populat)
66         heapq.heappush(populat,toclone)
67     elif p==1: # the current copy is evolved without cloning
68         Deltat=random.expovariate(sescape(1-state)) # interval until next evolution
69         toclone=(t+Deltat,Deltat,1-state)
70         heapq.heappush(populat,toclone)
71     else: # p>1 : make p clones ; population size becomes N+p-1 ; remove p-1 clones uniformly
72         pcount=p
73         while pcount>0:

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73         pcount-=1
74         Deltat=random.expovariate(sescape(1-state)) # interval until next evolution
75         toclone=(t+Deltat,Deltat,1-state)
76         heapq.heappush(populat,toclone)
77         # we first chose uniformly the p-1 distinct indices to remove, among the N+p-1 indices
78         listsize=popsiz+p-1;indices=random.sample(xrange(listsize),p-1)
79         # the list of indices to remove is sorted from largest to smallest, so as to remove largest
80         indices first
81         indices.sort(reverse=True)
82         for i in indices:
83             heapq_remove(populat,i)
84
85     if t>tmin:
86         Yint+=math.log((popsiz+p-1)/(1.*popsiz))
87         Y +=math.log((popsiz+cloningfactor-1)/(1.*popsiz))
88         if step%5 == 0:
89             sampletime.append(t)
90             samplesY.append(Y)
91             samplesYint.append(Yint)
92             step+=1
93 # Bulk numerical estimation of psiK(s) from population size ~ e^(t psiK(s) )
94 psiK=Y/(t-tmin)
95 psiKint=Yint/(t-tmin)
96
97 # better estimation by fitting log(popsiz(t)) starting from a given threshold so as to isolate the
98 # exponential behaviour popsiz(t) ~ e^(t psiK(s) )
99
100 psiKintfit,const = pylab.polyfit(sampletime,samplesYint,1)
101 psiKfit,const = pylab.polyfit(sampletime,samplesY, 1)
102
103 print 'final total population size = ', len(populat)
104 print ' theoretical psi(s) = ', -.5+.5*math.sqrt(1.-4.*c*(1.-c)*(1.-math.exp(-2.*s)))
105 print ' bulk numerical psi(s) = ', psiK
106 print '(int) bulk numerical psi(s) = ', psiKint
107 print 'fitted numerical fit psi(s) = ', psiKfit
108 print '(int) ----- fit psi(s) = ', psiKintfit
109
110 pylab.plot(sampletime,samplesY, 'r')
111 pylab.plot(sampletime,samplesYint, 'b')
112 pylab.plot(sampletime,[const+psiKfit*sampletime[i] for i in range(len(sampletime)) ], 'g-')
113 pylab.show()
114

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