

```

1  ### Cloning_randomtimes_tmax.py
2  ### When cloning, the time is now drawn differently for each new copy.
3
4  import random, math, pylab, heapq
5      # heapq provides the Heap Queue structure which allows to manipulate efficiently
   sorted list.
6      # Here we use a list of copies of the system, sorted according to their next time of
   evolution.
7  c=.25      # c = creation rate 0->1 ; 1-c = annihilation rate 1->0
8  s=-0.02    # s conjugated to the activity K ; this algorithm works for s<0
9  populat=[(0.,.1,0)]
10     # initial state of the population :
11     # each member of (or "copy" in) the population is described by a pair
   (time,dt,state)
12     #   time = next time at which it will evolve
13     #   dt = time since last evolution
14     #   state = 0 or 1 = empty or occupied
15 t,tmax=0.,1300. # initial and maximal time
16 step=0      # counter for the number of steps in the "mutation/selection" process
17
18 # s-modified escape rate
19 def sescape(n):
20     if n==0:
21         esc=c*math.exp(-s)
22     else:
23         esc=(1-c)*math.exp(-s)
24     return esc
25
26 def cloningrate(n): # always positive, as we took s<0
27     if n==0:
28         rate=c*(math.exp(-s)-1.)
29     else:
30         rate=(1.-c)*(math.exp(-s)-1.)
31     return rate
32
33 # lists to sample the logarithm of the population size a function of time
34 sampletime,samplespop=[],[]
35
36 heapq.heapify(populat) # orders the population into a Heap Queue ; useful if the initial state of
   the population contains more than one copy
37 while t<tmax:
38     (t,dt,state)=heapq.heappop(populat) # pops and yields the first element of populat, which is
   always the next to evolve
39     p=int( math.exp(dt*cloningrate(state)) + random.random() ) # the copy we popped out is to be
   replaced by p copies
40     while p>0:
41         p-=1
42         Deltat=random.expovariate(sescape(1-state)) # interval until next evolution
43         toclone=(t+Deltat,Deltat,1-state)
44         heapq.heappush(populat,toclon)
45         step+=1
46         if step%10 == 0:
47             sampletime.append(t)
48             samplespop.append(math.log(len(populat)))
49
50 # Bulk numerical estimation of psiK(s) from population size ~ e^(t psiK(s) )
51 psiK=math.log(len(populat))/t
52
53 # better estimation by fitting log(popsizet) starting from a given threshold so as to isolate the
   large-time exponential behaviour popsizet ~ e^(t psiK(s) )
54 Nsamples=len(sampletime)
55 threshold=Nsamples/2
56 psiKfit,const = pylab.polyfit(sampletime[threshold:],samplespop[threshold:],1)
57
58 print 'final total population size = ', len(populat)
59 print '    theoretical psi(s) = ', -.5+.5*math.sqrt(1.-4.*c*(1.-c)*(1.-math.exp(-2.*s)))
60 print '    bulk numerical psi(s) = ', psiK
61 print 'fitted numerical fit psi(s) = ', psiKfit
62
63 pylab.plot(sampletime,samplespop, 'r')
64 pylab.plot(sampletime,[const+psiKfit*sampletime[i] for i in range(Nsamples) ], 'g-')
65 pylab.show()
66
67
68

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