

# Dynamics of domain walls with an internal degree of freedom

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Grenoble – LiPhy – 14th April 2014

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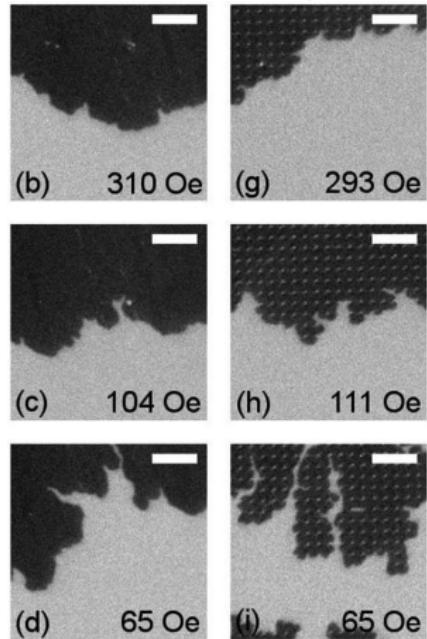
<sup>4</sup>Département de Physique Théorique et Section de Mathématiques, Genève

<sup>5</sup>CNEA, Bariloche, Argentina

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# Interfaces

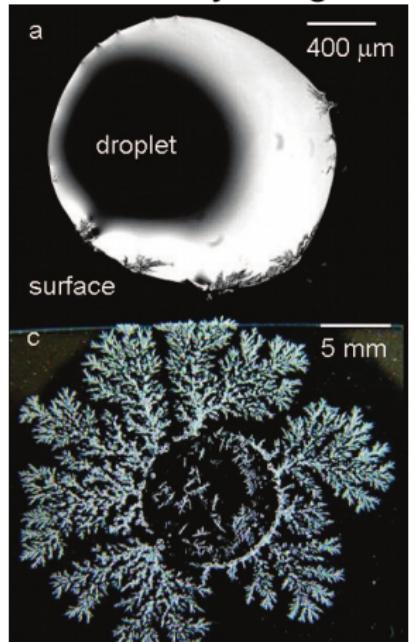
## Interfaces in magnetic films



Large range of physical scales

Wide spectrum of phenomena

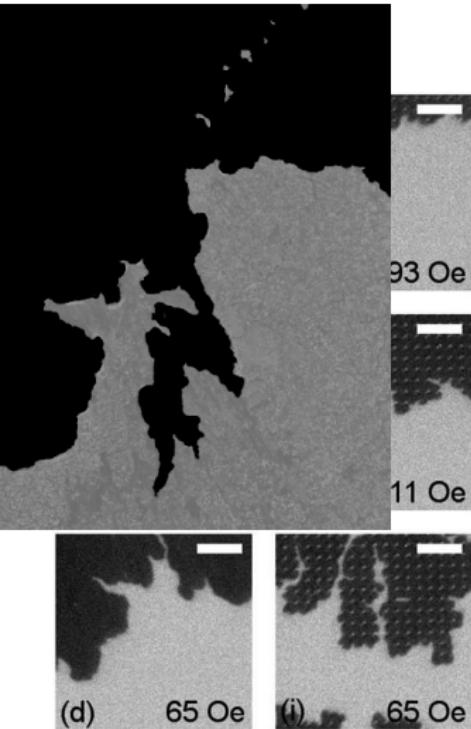
## Crystal growth



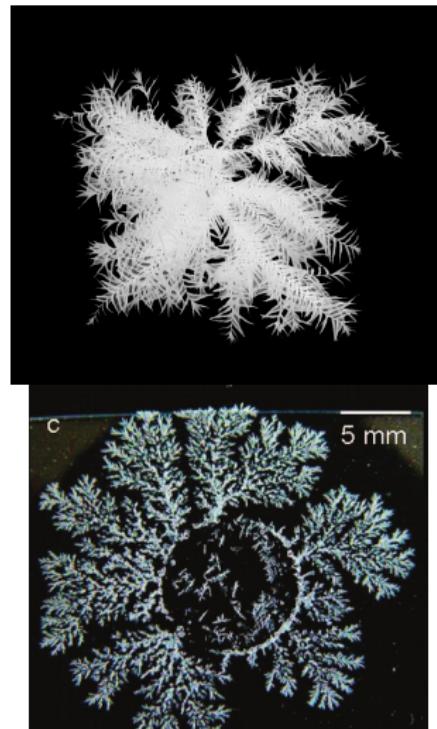
from Metaxas *et al.*

from Shahidzadeh-Bonn *et al.*

# Interfaces



Large range of physical scales



Wide spectrum of phenomena

from Metaxas *et al.*

from Shahidzadeh-Bonn *et al.*

# Interfaces







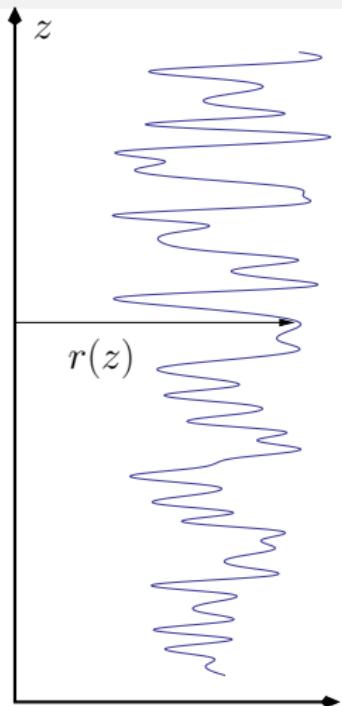
# Disordered elastic systems

- Elasticity: tends to **flatten** the interface

$$\frac{c}{2} \int dz (\nabla r(z))^2$$

- Disorder: tends to **bend** it

$$\int dz V(r(z), z)$$

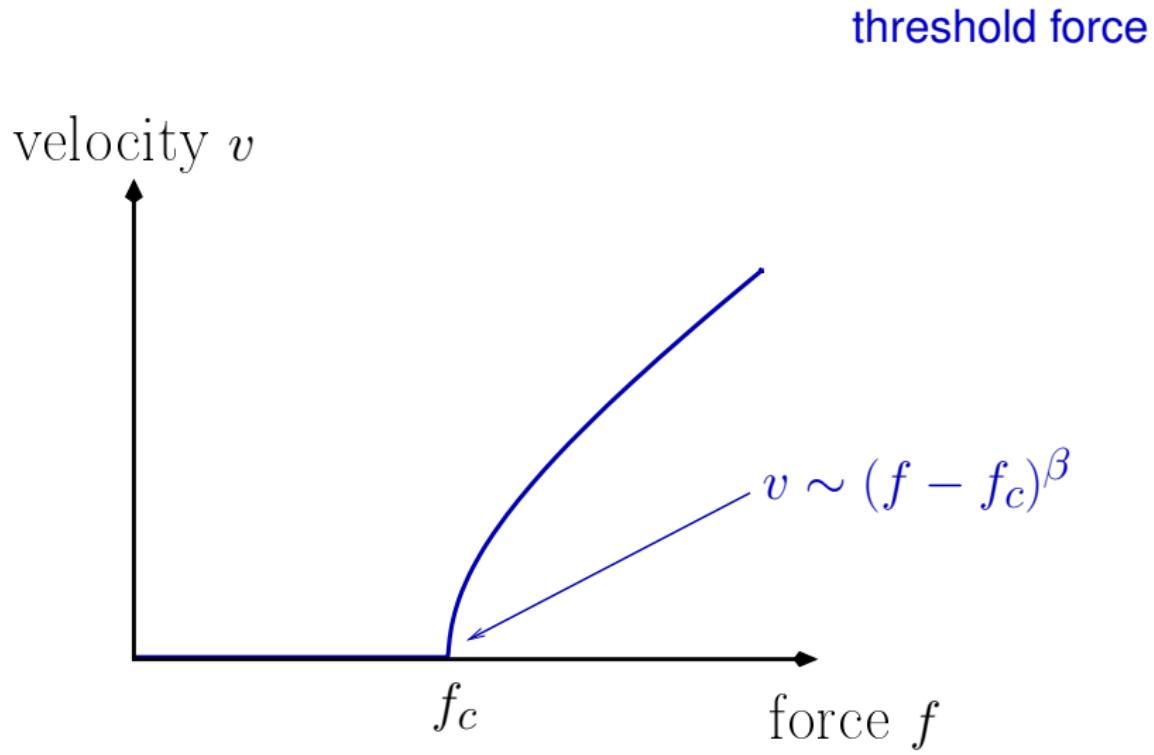


Competition btw “order” and “disorder”

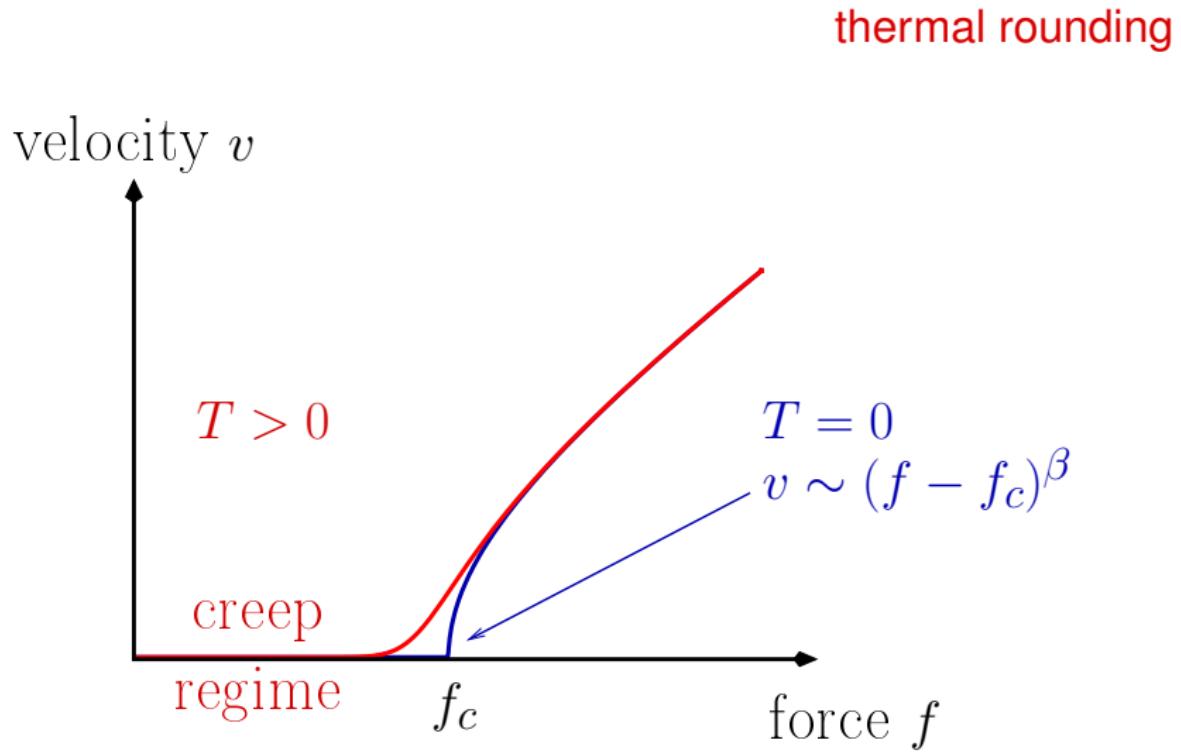
# Is the knowledge of $r(z)$ sufficient?

→ Have a look to the dynamics in simple examples.

# Depinning transition @ zero temperature



# Depinning transition @ finite temperature



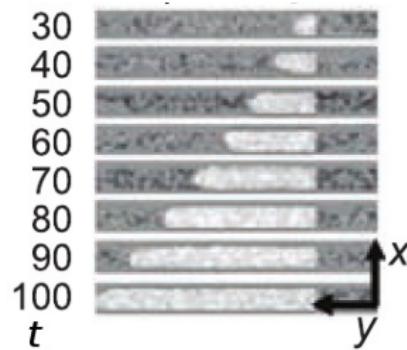
# Outline

## ① Interface Physics

- Systems
- Depinning transition

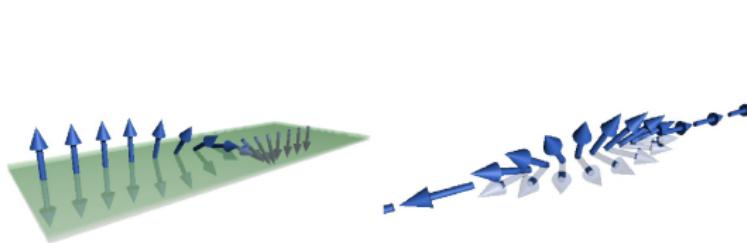
## ② Depinning with internal degree of freedom

- Modelisation
- Dynamics

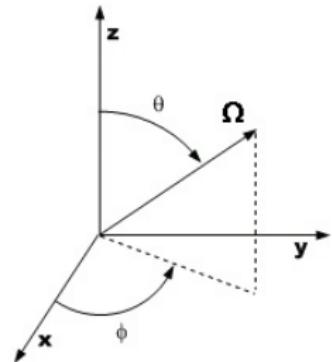


from Yamanouchi *et al.*, Science **317** 1726 (2007)

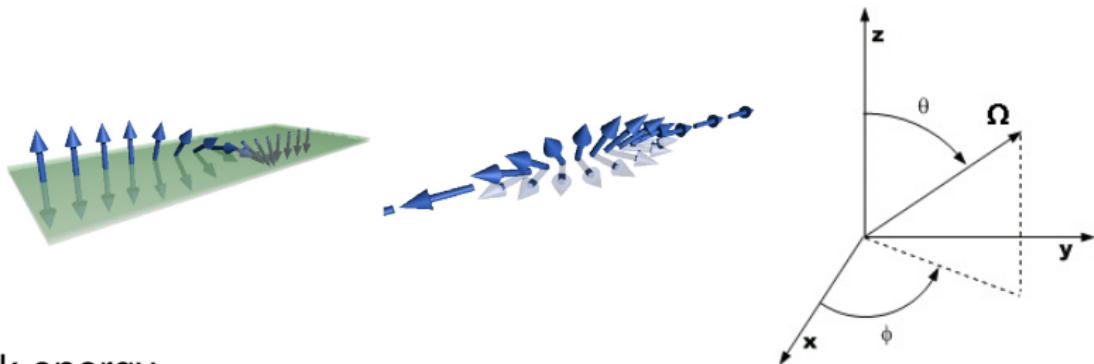
# Bulk model



from Tatara *et al.*, J. Phys. Soc. Jap 77 031003 (2008)



# Bulk model



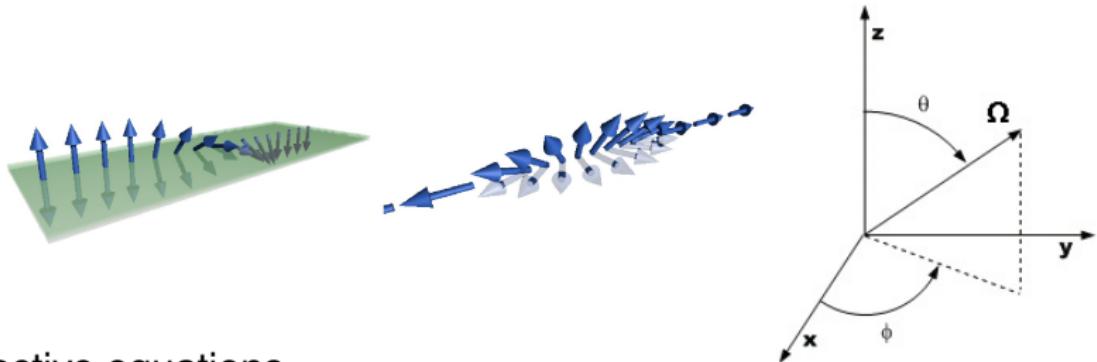
- Bulk energy

$$E = \int d^d x \left\{ J \left[ (\nabla \theta)^2 + \sin^2 \theta (\nabla \phi)^2 \right] + K \sin^2 \theta + K_{\perp} \sin^2 \theta \cos^2 \phi \right\}$$

- Equation of motion (Landau-Lifshitz-Gilbert)

$$\partial_t \Omega = \Omega \times \left( \frac{\delta E}{\delta \Omega} + f + \eta \right) - \Omega \times (\alpha \partial_t \Omega)$$

# Bulk model

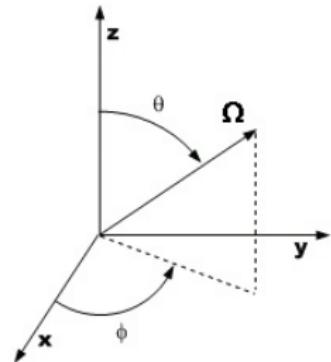
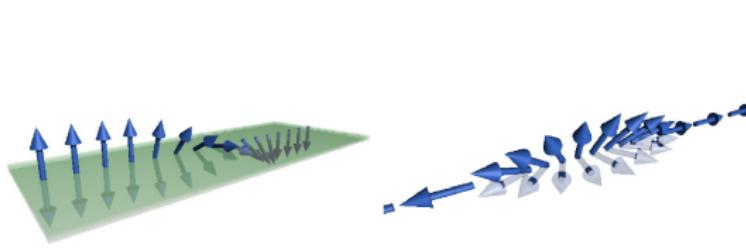


- Effective equations

$$\alpha \partial_t r - \partial_t \phi = J(\nabla r)^2 + F_{\text{pinning}} + f_{\text{ext}} + \eta_1$$

$$\alpha \partial_t \phi + \partial_t r = J(\nabla \phi)^2 + -\frac{1}{2} K_{\perp} \sin 2\phi + \eta_2$$

# Bulk model



- Rigid wall approximation

$$\alpha \partial_t r - \partial_t \phi = \underbrace{-\cos \kappa r}_{\text{pinning}} + \underbrace{f}_{\text{external}} + \eta_1$$

$$\alpha \partial_t \phi + \partial_t r = -\frac{1}{2} K_{\perp} \sin 2\phi + \eta_2$$

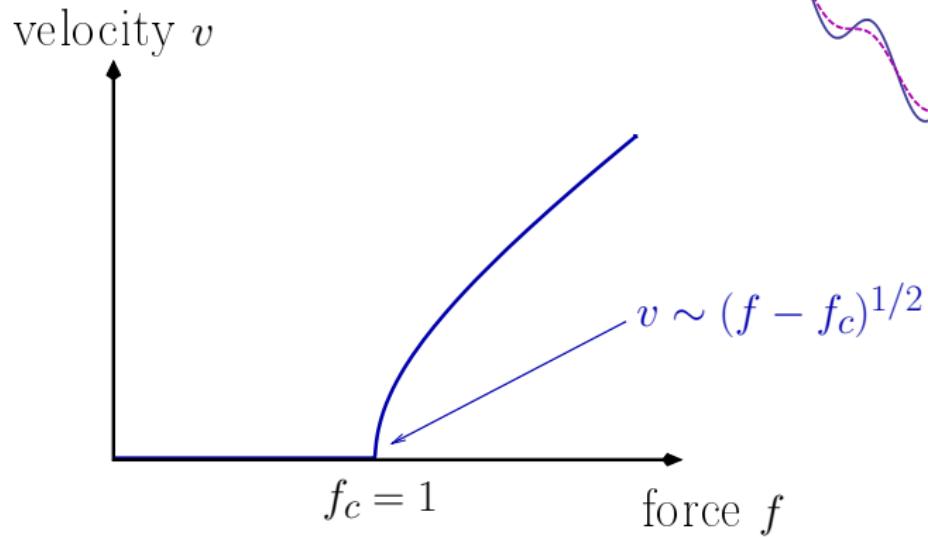
- Effective model

Position  $r(t)$  coupled to phase  $\phi(t)$

# Depinning @ zero temperature

(1<sup>st</sup> case) Large  $K_{\perp}$ :  $\phi$  decouples from  $r$

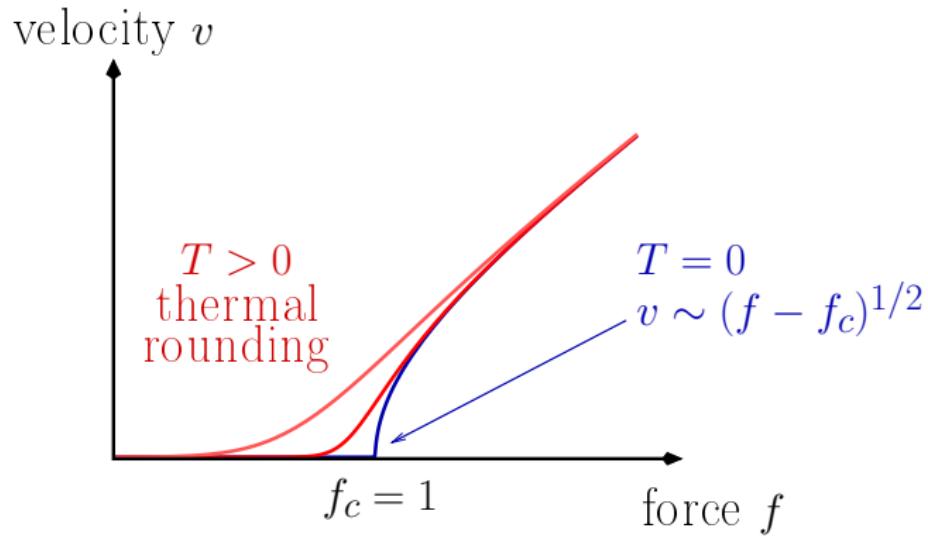
$$\alpha \partial_t r = f - \cos \kappa r$$



# Depinning @ finite temperature

(1<sup>st</sup> case) Large  $K_{\perp}$ :  $\phi$  decouples from  $r$

$$\alpha \partial_t r = f - \cos \kappa r + \eta$$



# Depinning @ zero temperature

(2<sup>nd</sup> case) Small  $K_{\perp}$ :  $\phi$  matters

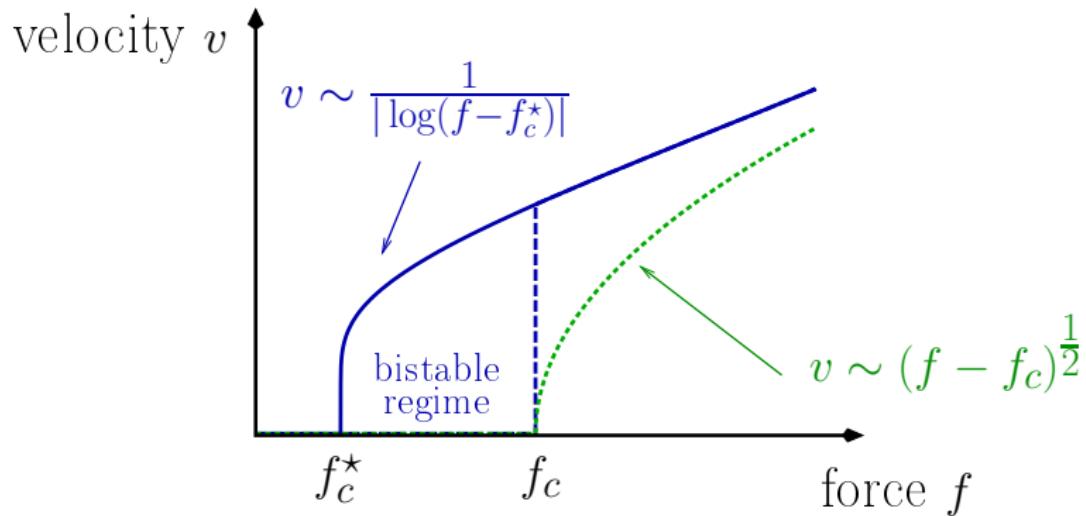
$$\alpha \partial_t r - \partial_t \phi = f - \cos \kappa r$$

$$\alpha \partial_t \phi + \partial_t r = -\frac{1}{2} K_{\perp} \sin 2\phi$$

# Depinning @ zero temperature

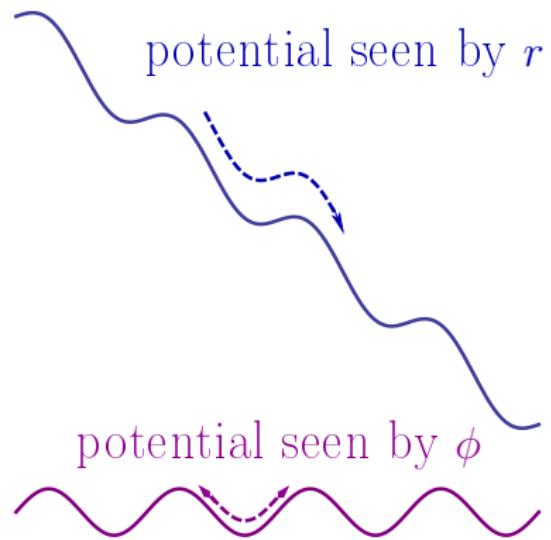
**(2<sup>nd</sup> case)** Small  $K_{\perp}$ :  $\phi$  matters

- Dramatic change in the depinning law:  $v \sim \frac{1}{|\log(f-f_c^*)|}$

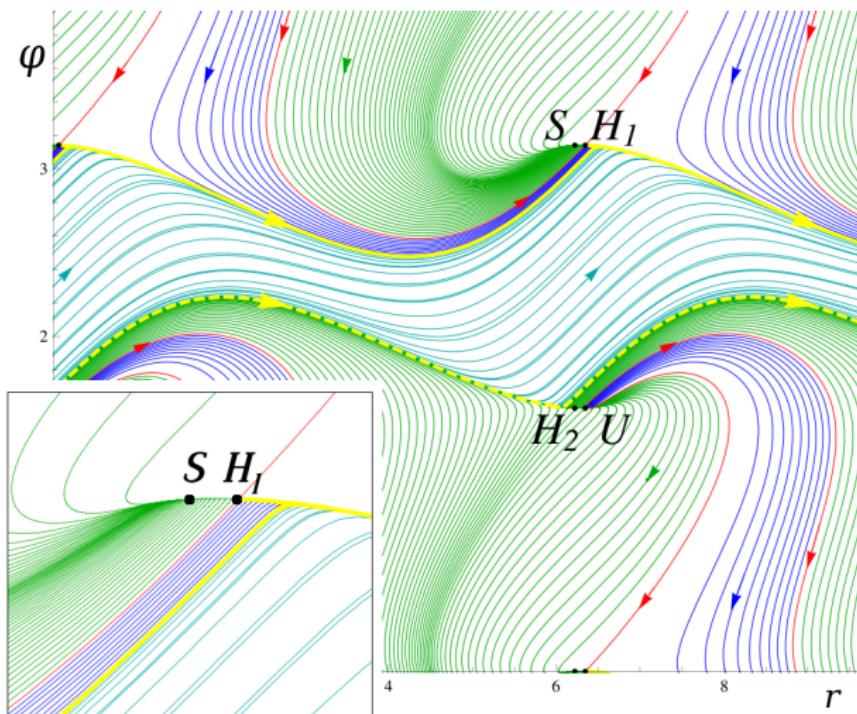


- Depinning at **lower** critical force:  $f_c^* < f_c$
- Bistability

# Physical interpretation



# Phase space

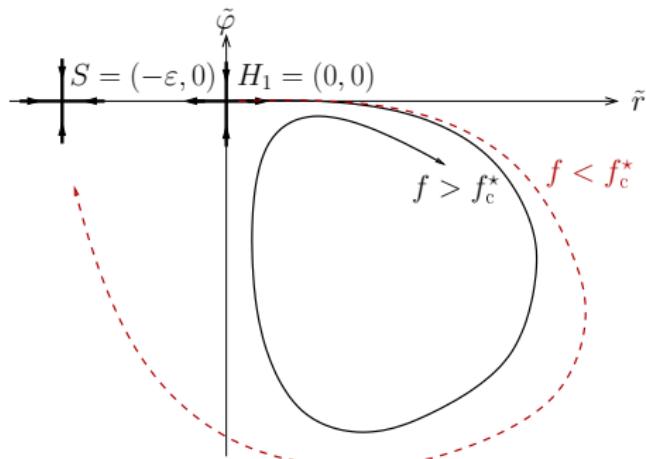


In the bistable regime ( $f_c^* < f < f_c$ )

# Phase space

Homoclinic bifurcation:

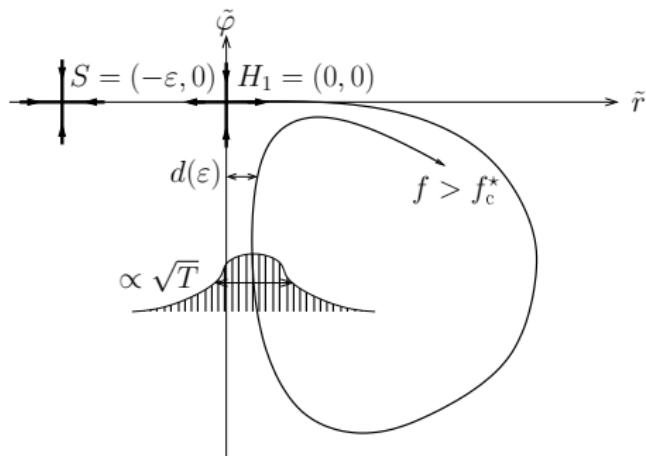
$$(\epsilon \propto f_c - f)$$



# Phase space: $T > 0$

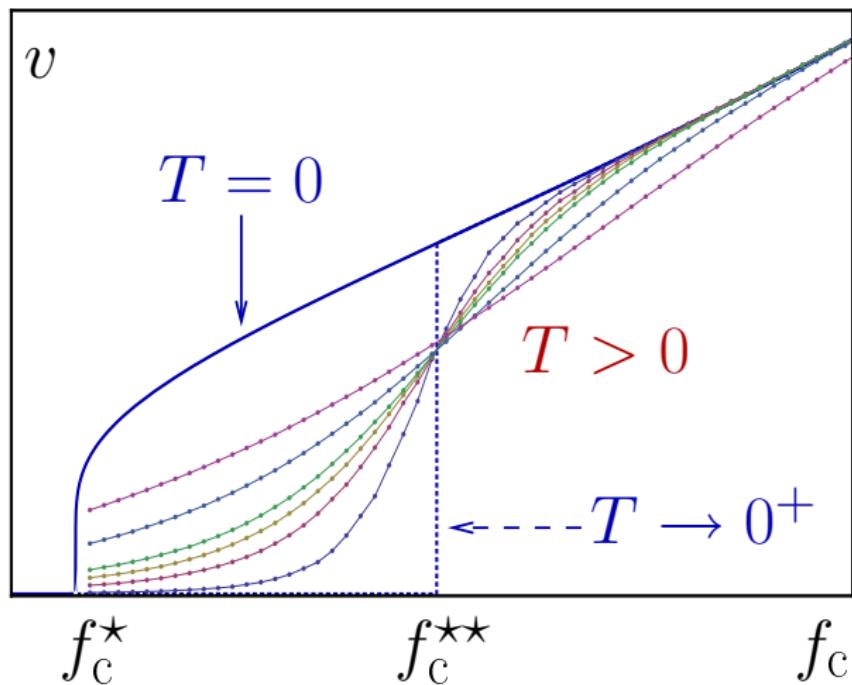
Homoclinic bifurcation with noise:

$$(\epsilon \propto f_c - f)$$



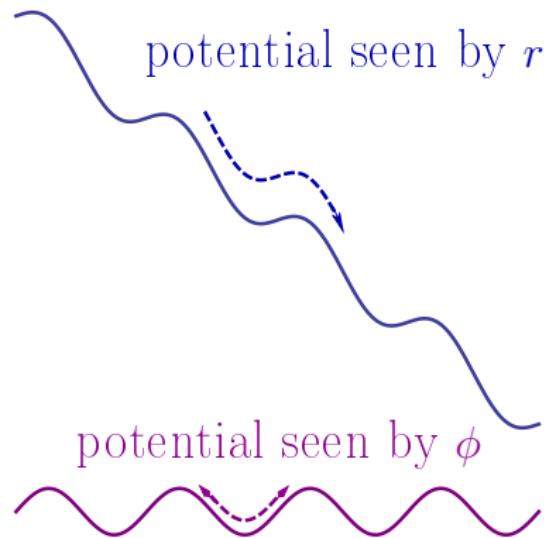
$$\text{escape time} \sim \underbrace{\exp\left(\frac{\epsilon^3}{T}\right)}_{\text{Arrhenius}} \underbrace{\exp\left(-\frac{A}{T}d(\epsilon)^2\right)}_{\text{Trapping probability}}$$

# Finite temperature



Force-velocity characteristics

This is not the end of the story

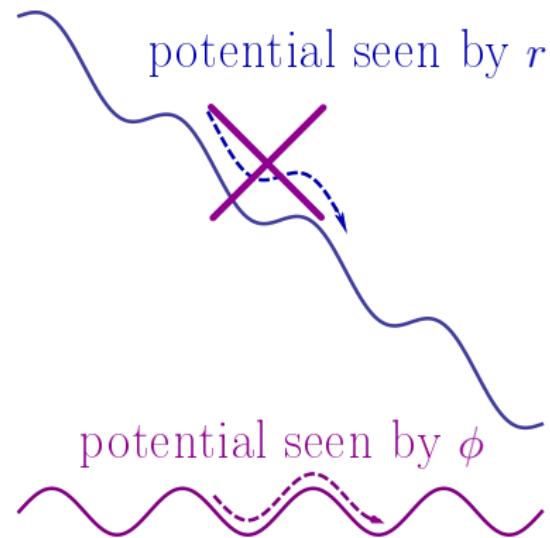


The phase  $\phi$  plays the role of inertia:

helps to cross barriers

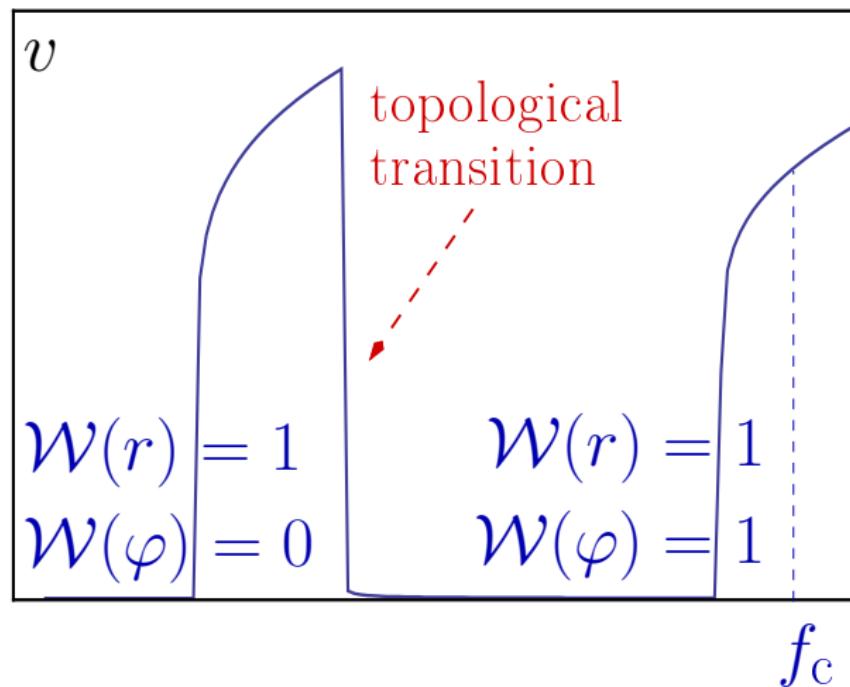
This is not the end of the story

**(3<sup>rd</sup> case) Even smaller  $K_\perp$**



inertia is unbounded whereas  $\phi$  is bounded and periodic

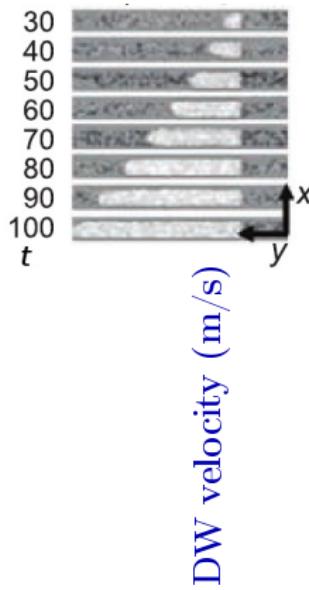
# Topological transition



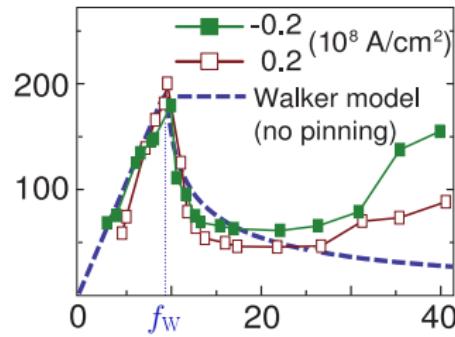
Successive regimes characterized by winding numbers  $\mathcal{W}$

## Experiment (i)

## SPINTRONICS

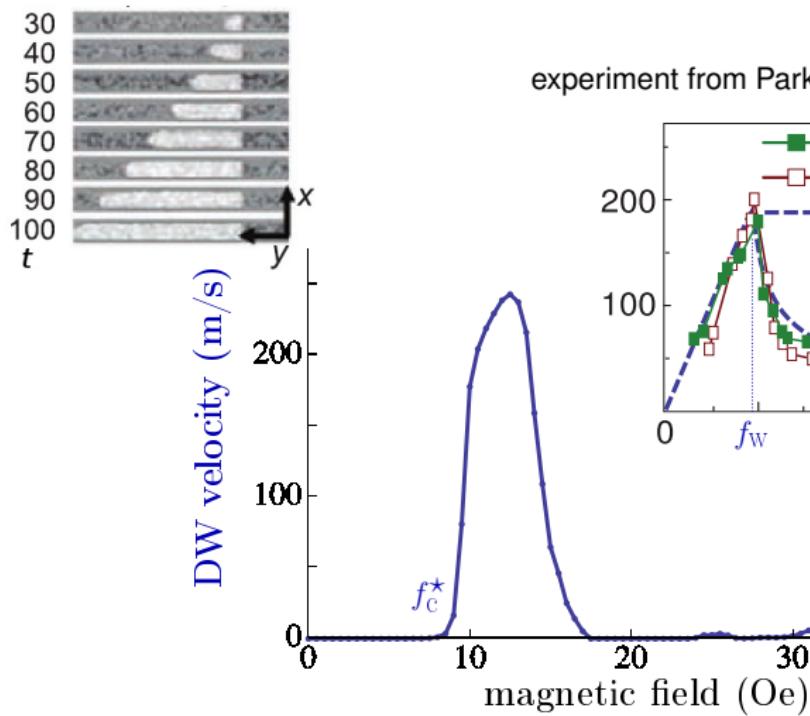


experiment from Parkin *et al.*, Science **320** 190 (2008)

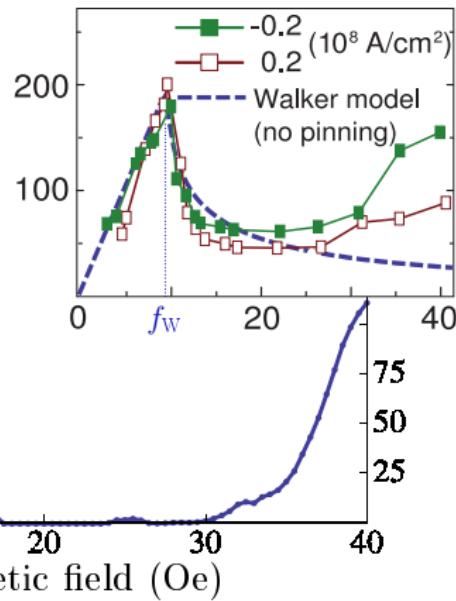


## Experiment (i)

## SPINTRONICS

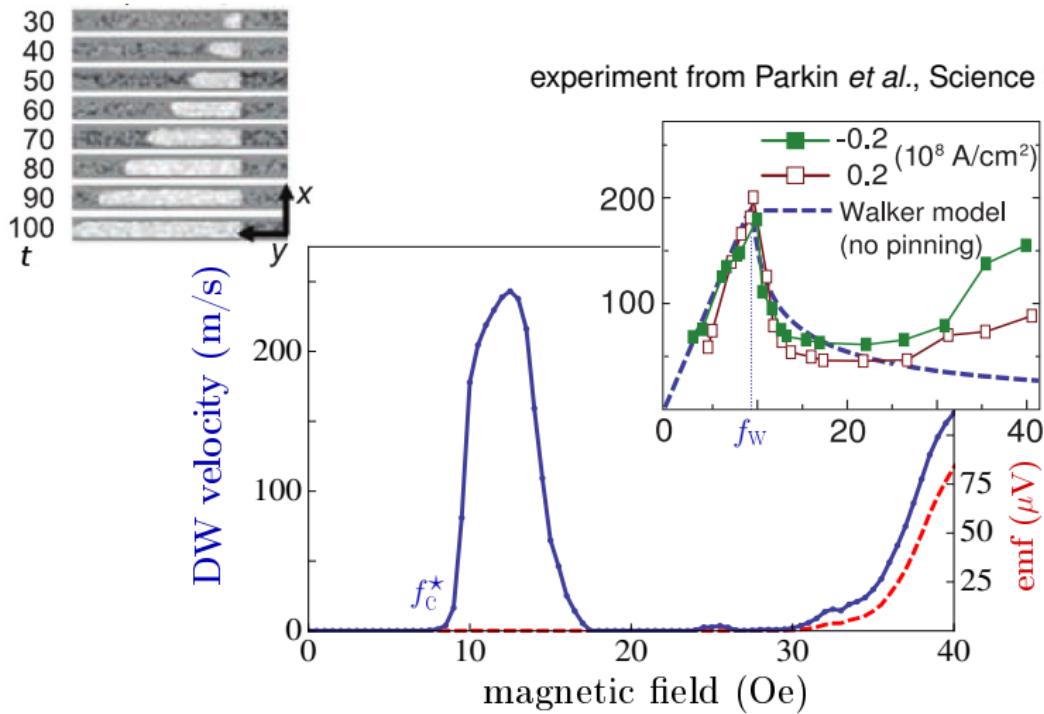


experiment from Parkin *et al.*, Science **320** 190 (2008)



## Experiment (i)

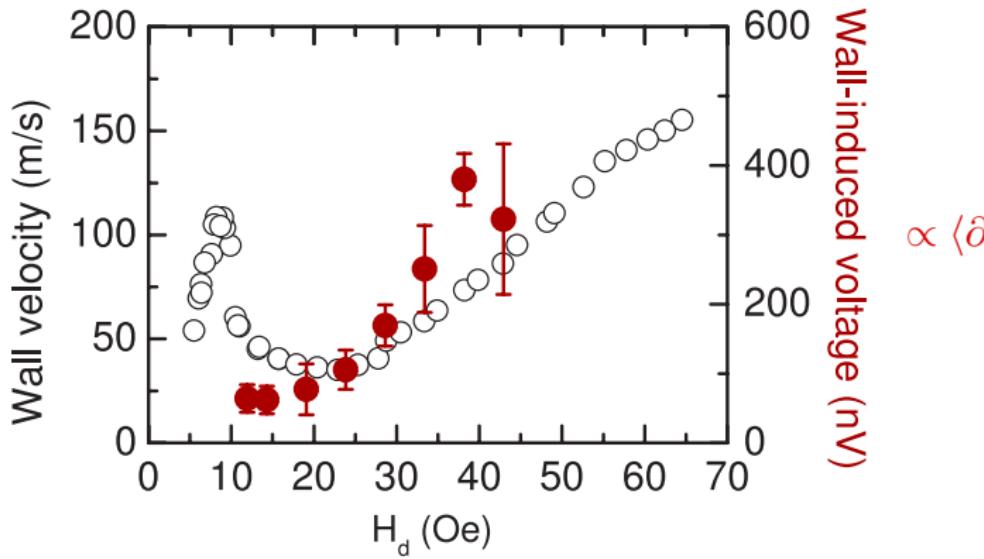
## SPINTRONICS



emf =  
wall  
induced  
voltage  
 $\propto \langle \partial_t \phi \rangle$

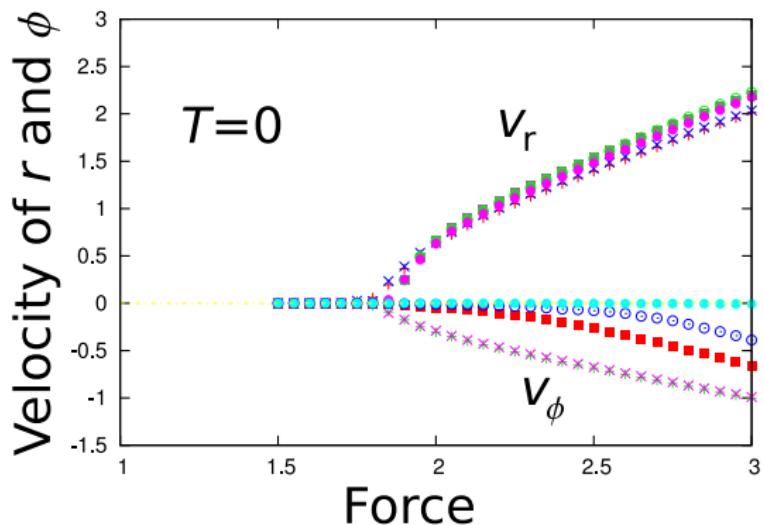
## Experiment (ii)

## SPINTRONICS

experiment from Yang, Beach *et al.*, PRL 102 067201 (2009)

# Numerics: including elasticity

on-going work with S. Bustingorry, A. Kolton



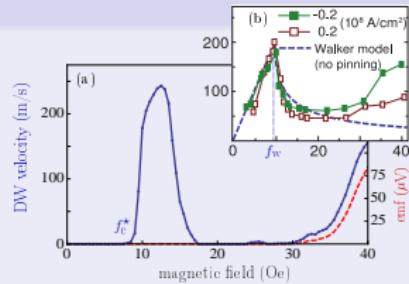
$T = 0$  creep-like motion of  $\phi$  induced by  $v_r > 0$

# Outlook

PRB **80** 054413 (2009)

## Internal degree of freedom

- unusual depinning law
- bistability
- non-monotonous  $v(f)$  at finite T
- link with experiments



## Perspective

- Interface with elasticity
- Current driven wall
- Experiments
- Other internal degrees

↔ modified creep law?

↔ periodic patterning?

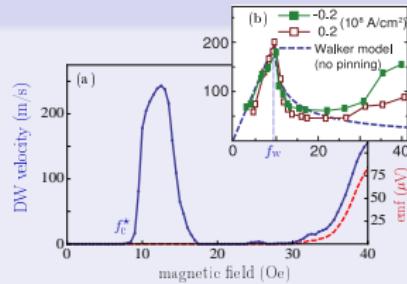
↔ coupled interfaces?

# Outlook

PRB **80** 054413 (2009)

## Internal degree of freedom

- unusual depinning law
- bistability
- non-monotonous  $v(f)$  at finite T
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## Perspective

- Interface with **elasticity**  $\longleftrightarrow$  modified creep law?
- **Current** driven wall
- Experiments  $\longleftrightarrow$  periodic patterning?
- Other internal degrees  $\longleftrightarrow$  coupled interfaces?